# Relevance of the Eigenstate Thermalization Hypothesis for Thermal Relaxation

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#### Sao Carlos, Feb. 25th, 2015

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## Facts, Notions, Concepts (and cups of coffee....)

Temperature differences between macroscopic objects in energy exchanging contact are expected to vanish, irrespective of their initial values.

• Eigenstate Thermalization Hypothesis (ETH): "cloud width"  $\Sigma(\hat{D},\hat{H})$  small

$$\Sigma^2 \equiv \sum_{n=1}^d p_n \langle n | \hat{D} | n \rangle^2 - \bar{D}^2 \quad \bar{D} \equiv \sum_{n=1}^d p_n \langle n | \hat{D} | n \rangle \quad \hat{H} | n \rangle = E_n$$

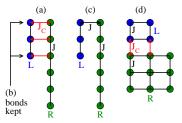
 $p_n$  probability distribution, sharply peaked at some  $E_n = \bar{E}$ 

- Initial state independence (ISI): Expectation values of some observable  $\hat{D}$  relax towards a common value irrespective of their initial values.
- non-resonance condition (NRC): any difference between two eigenvalues of  $\hat{H}$  occurs only once.
- Given the NRC holds and the ETH applies  $\Rightarrow$  ISI follows for all possible initial states with sufficiently broad energy distributions
- If the ETH does not apply there may or may not be ISI, depending on the initial state.

Is the ETH (in the above sense) physically imperative for ISI of energy differences?

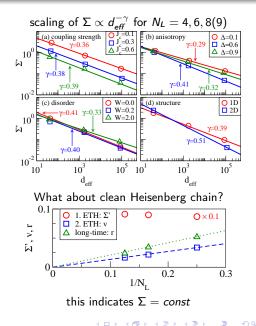
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model: weakly coupled, anisotropic Heisenberg chains,  $N_R = 2N_L$ 



pieces of the Hamiltonian:  $\hat{S}_x^{\alpha} \hat{S}_x^{\beta} + \hat{S}_y^{\alpha} \hat{S}_y^{\beta} + \Delta \hat{S}_z^{\alpha} \hat{S}_z^{\beta} + B_{\alpha} \hat{S}_z^{\alpha}$ 

**observable:** energy difference:  $\hat{D} = \hat{H}_L - \hat{H}_R$ 



What initial state?  $\Rightarrow$  microcanonical observable displaced state (MOD) (no "quench")

$$\hat{
ho}(\mathbf{0})=
ho_{\mathsf{MOD}}(\chi,\sigma,d'):\propto e^{-(\hat{H}^2+\chi^2[\hat{D}-d'^2])/2\sigma^2}$$

choosing  $\chi, \sigma, d'$  carefully we are able to prepare states with  $\Delta E \approx 0.3$  and  $d(0) = \pm N_L$  with  $d(t) := \langle \hat{D}(t) \rangle$  (overall energy scale ca.  $3N_L$ )

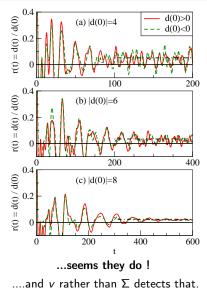
"stick effect": it looks like  $d(t) \rightarrow r(N_L)d(0)$  where  $r(N_L)$  is a constant which is independent of d(0)Does the stick effect vanish with increasing size?

Besides,  $\boldsymbol{\Sigma}$  is not a dimensionless quantity, so what is "small"?

Define, just for fun:  $v^2 = \Sigma^2/\delta^2$  with

$$\delta^2 = \langle \hat{D}^2 \rangle_0 - \langle \hat{D} \rangle_0^2$$

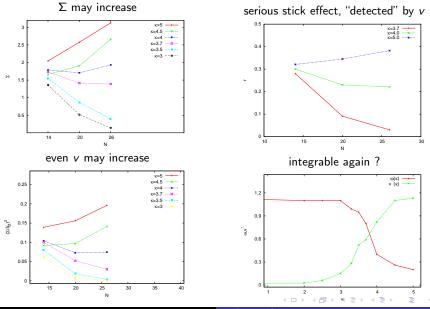
with  $\langle \cdots \rangle_0 = \operatorname{Tr} \{ \cdots \hat{\rho}_{MOD}(\chi = 0, \sigma, d') \}$ 



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## What about strong couplings?

Same model (a), strong interchain couplings  $J_c = (3...5)J$ 



J.Gemmer Relevance of ETH

# Thank you for your attention!

The talk itself as well as related papers from our group may be found on our webpage.

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